Assignment #2
Date Due: June 7, 2022
Total: 100 marks

1. (20 marks) We denote by

   $L_1 = \{$the set of all strings over the alphabet $\{0, 1, 2\}$ that begin with $0101\}$

   $L_2 = \{$the set of all strings over the alphabet $\{0, 1, 2\}$ that end with $10111\}$

   $L_3 = \{$the set of all strings over the alphabet $\{0, 1, 2\}$ that begin with $01001\}$

   Give a regular expression for the following language over the alphabet $\{0, 1, 2\}$:

   (a) $L_4 = L_1 \cap L_2$, and

   (b) $L_5 = L_3 \cap L_2$

2. (20 marks) Find the regular expression for the language

   $L_7 = \{w \in \{0, 1, 2\} \mid w$ starts with010 and ends in $1011\}$

   Transform the regular expressions into an equivalent ε-NFA, and afterwards in a DFA, using the algorithms learned in class (or the ones in your textbook).

   Minimize the resulting DFAs.

3. (40 marks) Give a regular expression for each of the following languages over the alphabet $\{0, 1, 2\}$:

   (a) the set of all strings consisting of alternating groups of 11 and 120 (11 and 120 *alternates* at least once);

   (b) the set of all strings whose fourth symbol from the right end is a 0;

   (c) the set of strings that either begin, or end (or both) with 1020;

   (d) the set of strings such that the number of 0's is divisible by six, and the number of 2's is not divisible by seven.

4. (20 marks) Write regular expressions for the following languages over the alphabet $\Sigma = \{0, 1, 2, 3, 5\}$:

   (a) the set of all strings beginning with a 1, 3 or 5, that, when the string is interpreted as an integer in base 7, is a multiple of 6 plus 3. For example:

   - strings 3, 30, 555, 333, 50013, 50121, 33333, 5022, 50301, and 555552 are in the language;

- the strings 20, 00, 022, 0020, 37 , 23, 5057, 223, 2325, 2375, 5, 32222, 505, 22, 72, and 035 are not.

(b) The set of all strings that ends with an **1, 3, or 5** and when the string is interpreted *in reverse* as an integer **in base 8, is a multiple of 6 plus 3**. A Examples of strings in the language are 3, 03, 555, 333, 31005, 12105, 33333, 2205, 10305, and 255555 Examples of strings that are not in the language are: 02, 00, 220, 0200, 73 , 32, 7505, 322, 5232, 5732, 5, 22223, 505, 22, 27, and 530.

5. (25 marks) Consider the DFA with the following transition table:

	0	1
→ A	D	A
∗ B	C	B
C	B	C
∗ D	B	D

(a) (10 marks) Find the equivalent regular expression using the algorithms learned in class.

(b) (10 marks) Transform the regular expression into an ε-NFA

(c) (10 marks) Transform the ε-NFA into a DFA.

6. (10 marks) Check your results with Grail+ and comment on the Grail+ experiments(another 5 marks).